

11.4 Perpendicular Cross Sections

CA #2

Calculus

Name: _____

The base of an object is bounded by the lines $y = x^2 - 4$ and $y = 4 - 2x$. Find the volume of the object with the indicated cross sections taken perpendicular to the x -axis. Use a calculator after you set up the integral!

1. Squares

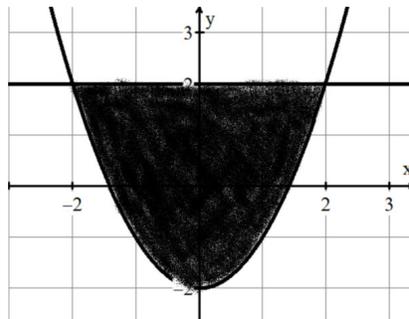
2. Equilateral triangles

3. Semi-circles

4. Isosceles right triangles (side is the base)

5. Set up the integral to find the area of the region bounded by $y = x^2 - 2$, and $y = 2$. DO NOT EVALUATE.

With respect to x .



With respect to y .

6. A solid is generated when the region in the first quadrant bounded by the graph of $y = 1 + \sin^2 x$, the line $x = \frac{\pi}{2}$, the x -axis, and the y -axis is revolved about the x -axis. What is the integral that represents the volume of the resulting solid of revolution?

Answers to 11.4 CA #2

1. $\int_{-4}^2 (-x^2 - 2x + 8)^2 dx = 355.2$	2. $\frac{\sqrt{3}}{4} \int_{-4}^2 (-x^2 - 2x + 8)^2 dx = 153.806$	
3. $\frac{\pi}{8} \int_{-4}^2 (-x^2 - 2x + 8)^2 dx = 101.7876$	4. $\frac{1}{2} \int_{-4}^2 (-x^2 - 2x + 8)^2 dx = 177.6$	
5a. $\int_{-2}^2 (4 - x^2) dx$	5b. $\int_{-2}^2 (2\sqrt{y+2}) dy$	6. $\pi \int_0^{\frac{\pi}{2}} (1 + \sin^2 x)^2 dx$